

# The meteoroid fluence at Mars due to Comet C/2013 A1 (Siding Spring): Two models

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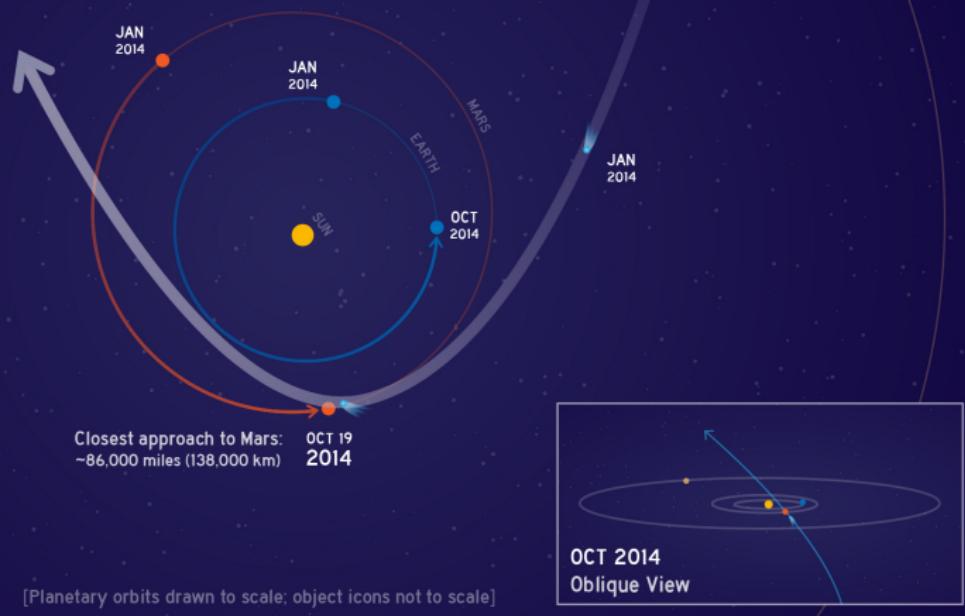


July 2, 2014

# NEAR MISS!

Comet Siding Spring (C/2013 A1) is racing toward Mars for a close encounter in October, 2014.

Image credit: NASA/JPL



# Spherical model

Quantifying the number of  $\gtrsim 100$  micron<sup>1</sup> particles:

- ① Determine brightness.
- ② Use particle albedo to compute the total particle surface area.
- ③ Use particle size distribution, bulk density to compute number of particles.
- ④ Use  $r^{-2}$  spatial distribution to compute the number density.
- ⑤ Integrate along the trajectory to get fluence.

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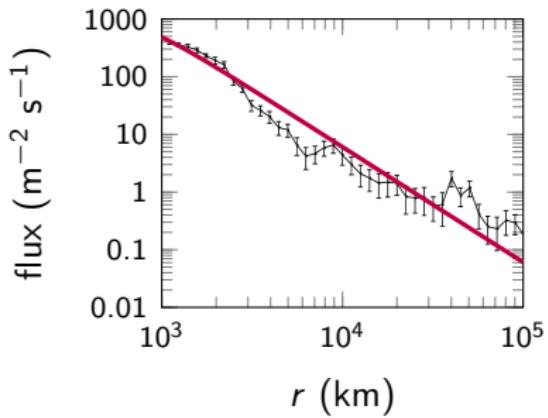
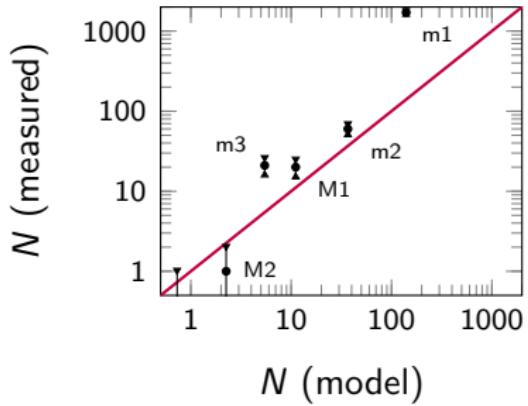
<sup>1</sup>100 micron particles are capable of cutting exposed spacecraft wires.

# Spherical model

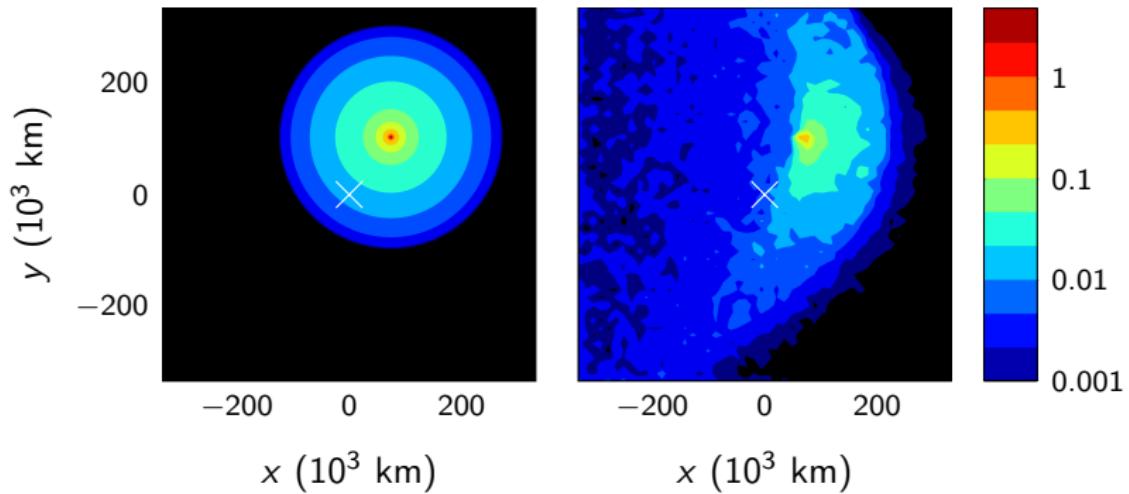
$$\begin{aligned}\sigma_* = & \frac{gh^{-\beta}}{a} \left(\frac{2}{\pi}\right)^{\frac{1}{3}} \left(\frac{\rho}{3}\right)^{\frac{2}{3}} 10^{-0.4(M1-m_{\odot,1\text{au}})} \text{ au}^2 \\ & \times \left(\frac{3-k}{1-k}\right) \left(\frac{m_{\max}^{(1-k)/3} - m_*^{(1-k)/3}}{m_{\max}^{(3-k)/3} - m_{\min}^{(3-k)/3}}\right) \\ & \times \frac{\cos^{-1}(b/r_c)}{b r_c}\end{aligned}$$

This analytic model can be used to quickly calculate new fluence estimates as comet properties are measured/constrained.

# Reproducing *Giotto* and *Stardust* results

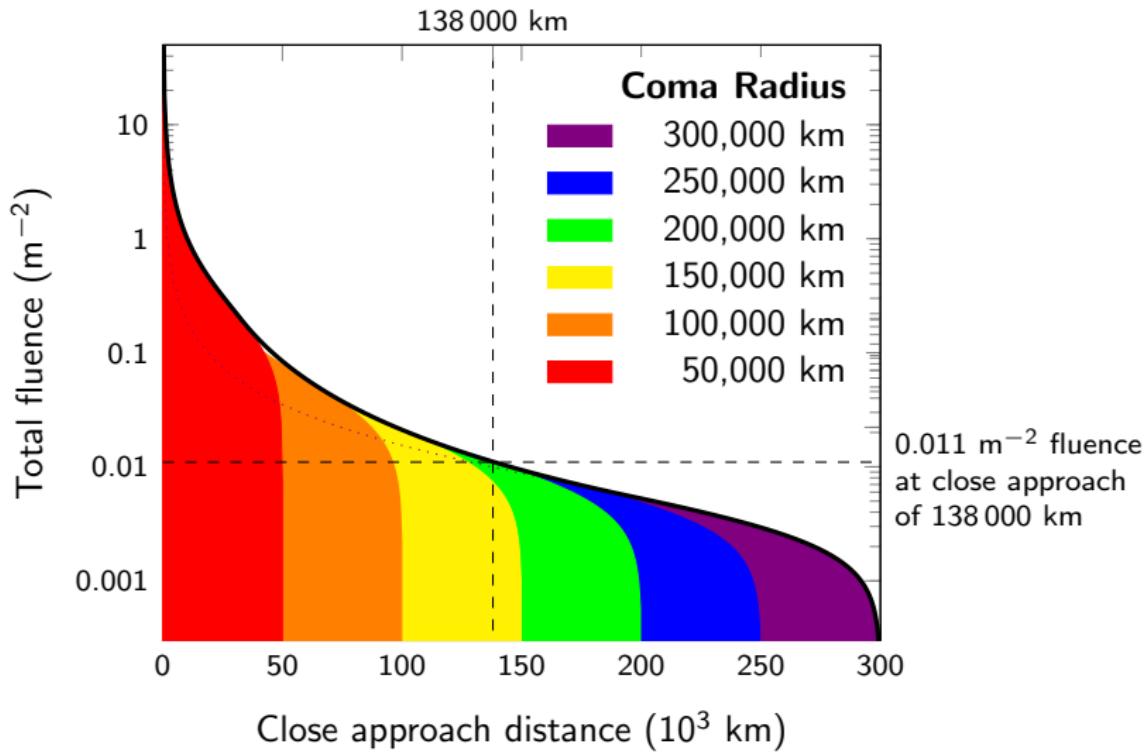
Halley data (Fulle et al., 2000), [our model](#)Wild 2 data (Tuzzolino et al., 2004), [our model](#)

# Comparison with simulations



Simulations illustrate (modest) deviance from spherical model due to coma asymmetry and tail.

## Dependence on coma size



# Quasi-Keplerian model

Trajectory:

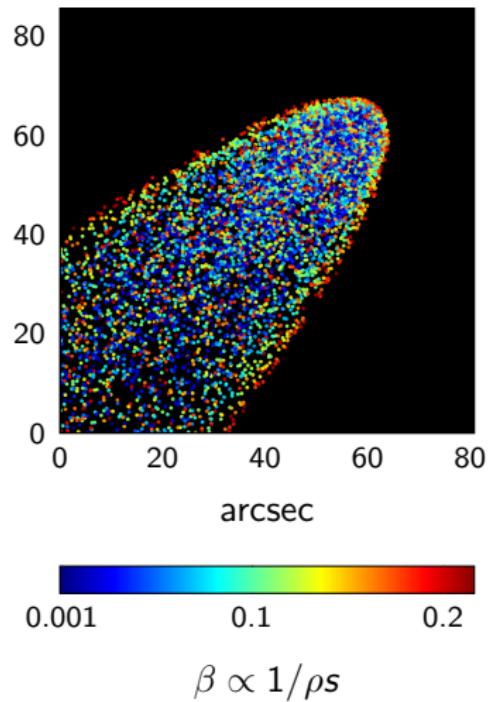
$$v_{ej} = v_0 \beta^{-\mu} r^{-\nu}$$

$$\vec{F} = -\frac{GMm}{r^2} (1 - \beta) \hat{r}$$

Particle distribution:

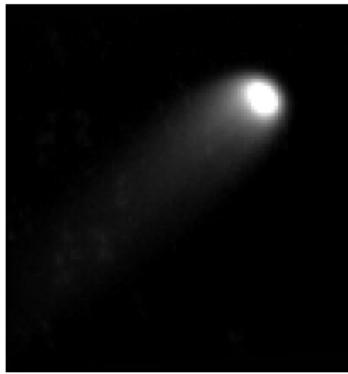
$$\frac{dN}{d\beta} \propto \beta^\alpha, \quad \frac{dN}{dr} \propto r^{-\gamma}$$

$$\frac{dN}{dv} \propto 1 - \left( \frac{v/v_{ej} - 1}{f_v} \right)^2$$



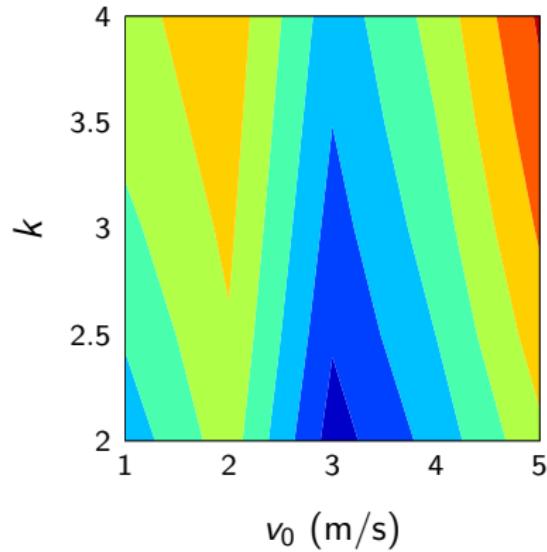
# Fit to observations

Using efficient algorithms to solve Kepler's equation (Gooding & Odell, 1988), we can simulate  $10^6$  particles in seconds:



We use Hubble images (Li et al., 2014) to fit for six parameters.

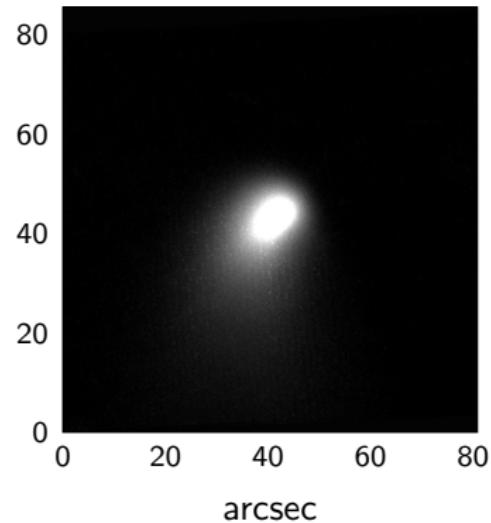
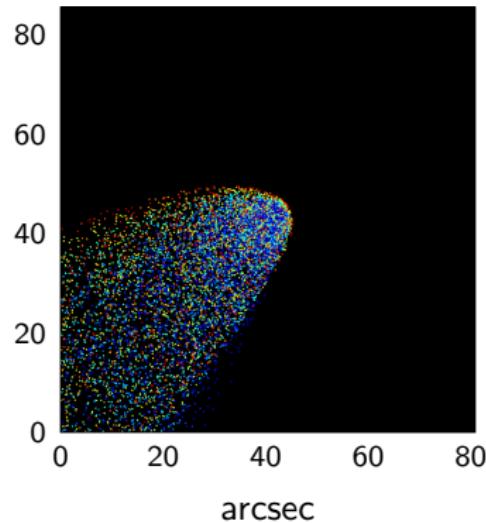
# Preliminary results



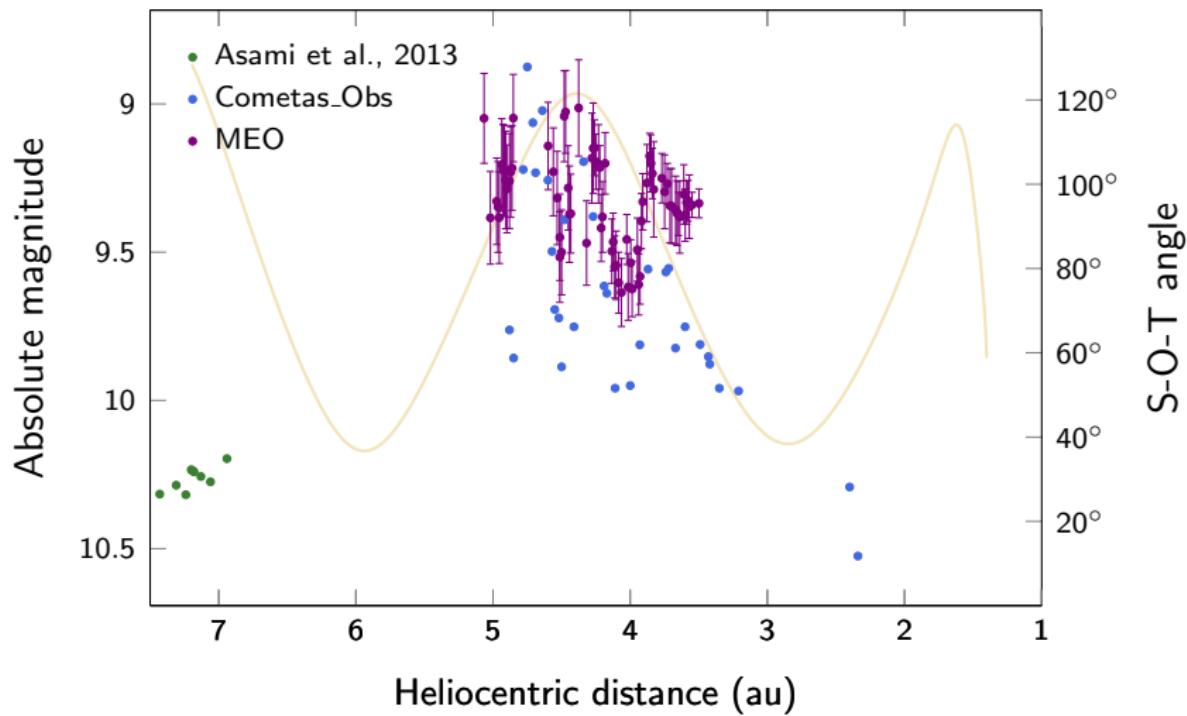
- Used a coarse, 6-d parameter grid
- Simultaneous fitting of all 3 Hubble observations
- Velocities  $\sim$  a few m/s
- Flat-to-inverted size distribution favored

# Size distribution

Comet's shape in October images requires large particles/small  $\beta$



# Incorporating additional observations



# Summary

We've developed two comet models:

- A spherical, analytic model that describes the particle distribution within the coma
  - Provides rough estimate of the meteoroid environment
  - Recreates Halley and Wild 2 particle counts to within an order of magnitude
  - No longer useful for Siding Spring at Mars
- A fast, quasi-Keplerian model that describes the particle distribution in the coma and tail
  - Can be combined with observations to fit for ejection velocity and particle distribution
  - Preliminary fit favors low velocity, flat/inverted size distribution
  - Future work: incorporate ground observations, apply to other monitored comets